

Security Enhancement of a Remote User Authentication Scheme Using Bilinear Pairings and ECC

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Abstract

Remote authentication is an important mechanism to control user access to remote systems and a password-based authentication is a preferable method. With advances in elliptic curve cryptography, Jia et al. [10] proposed a remote user authentication scheme with a smart card. Their scheme utilized bilinear pairings and an elliptic curve ElGamal encryption scheme to provide a secure authentication mechanism. However, we show that their scheme is vulnerable to our impersonation attack which any adversary can be authenticated successfully with probability 1 at no extra cost. We also suggest our provably secure improvement scheme which is verified to be more efficient from the point of computational complexity than the original scheme.

1. Introduction

Remote authentication over insecure communications is an important application of cryptographic protocols. The first construction, proposed by Lamport [11] in 1981, can resist against a replaying attack but it will be vulnerable if the verifier, who is holding the password table, is compromised. To overcome this weakness, several schemes [4, 5, 9, 13] have eliminated the use of the password table and utilized a smart card as an authentication token for users. A smart card provides a low cost communication, computation and convenience for users. In 2006, Das et al. [6] have proposed a novel remote authentication scheme with a smart card using bilinear pairings. This scheme allows users to choose their password freely and requires no password table for verifying the legitimacy of users. Later, Chow et al. [3] have presented a possible impersonation attack on the scheme [6] and also have provided a solution to fix the scheme. But, Goriparthi et al. [8], again, have in-

dicated that both Das's and Chow's schemes are vulnerable to forgery, replaying and insider attacks. Recently, Jia et al. [10] have utilized bilinear pairings along with the ElGamal version of elliptic curve cryptosystem in order to design a new remote authentication scheme withstanding the previous attacks. Nevertheless, in this paper, we show that Jia et al.'s authentication scheme is not secure by presenting our impersonation attack on their scheme. In addition, we point out the problem in Jia et al.'s construction and a method to fix it.

Organization: In the next section, we brief concepts of bilinear pairings and related security problems. We review Jia et al.'s scheme in Section 3 and propose an attack on the scheme in Section 4. An improvement scheme and its analysis are shown in Sections 5 and 6, respectively. Section 7 ends with concluding remarks.

2. Bilinear Pairings

Let G_1 and G_2 be additive and multiplicative groups of the same prime order q , respectively. Let P be a generator of G_1 . Assume that the discrete logarithm problems in both G_1 and G_2 are hard. Let $e : G_1 \times G_1 \rightarrow G_2$ be a pairing which satisfies the following properties:

Bilinear: $e(aP, bP') = e(P, P')^{ab}$ for all $P, P' \in G_1$ and all $a, b \in Z_q^*$.

Non-degenerate: If $e(P, P') = 1 \forall P' \in G_1$ then $P = \mathcal{O}$.

Computable: There is an efficient algorithm to compute $e(P, P')$ for any $P, P' \in G_1$.

Under such group G_1 , we can define the following hard cryptographic problems:

Discrete Logarithm (DL) Problem: Given $P, P' \in G_1$, find an integer n such that $P = nP'$ if such integer exists.

Computational Diffie-Hellman (CDH) Problem: Given a triple $(P, aP, bP) \in G_1$ for $a, b \in Z_q^*$, find $abP \in G_1$.

Decision Diffie-Hellman (DDH) Problem: Given a quadruple $(P, aP, bP, cP) \in G_1$ for $a, b, c \in Z_q^*$, decide

whether $c = ab \pmod{q}$ or not.

The CDH assumption states that there is no polynomial time algorithm can solve the CDH problem with non-negligible probability. Details about bilinear pairings and related problems can be found in [1, 2, 7].

3. Review of Jia *et al.*'s scheme [10]

Jia *et al.*'s scheme [10] scheme consists of four phases: setup, registration, authentication and password change, which are described below.

Phase 1: Setup

The remote server (RS) chooses an additive group G_1 and a multiplicative group G_2 of the same prime order q . P is a generator of the group G_1 . Let $e : G_1 \times G_1 \rightarrow G_2$ be a bilinear map and $H(\cdot) : \{0,1\}^* \rightarrow G_1$ be a cryptographic hash function. The RS selects a private key $s \in_R Z_q^*$ and computes its corresponding public key $P_{rs} = sP$. The server publishes the system parameters $\{G_1, G_2, e, q, P, P_{rs}, H\}$ while keeping s secret.

Phase 2: Registration

Step 2-1. A user U_i submits his identity ID_i and password pw_i to the RS.

Step 2-2. Upon receiving a request from U_i , the RS computes: $Reg_i = sH(ID_i) + H(pw_i)$

Step 2-3. The RS personalizes a smart card with the parameters: $\{ID_i, Reg_i, H(\cdot), P, P_{rs}\}$ and distributes the card to U_i over a secure channel.

Phase 3: Authentication

This phase includes user's login and RS's verification.

Step 3-1. The user U_i inserts the smart card into the input device and enters his identity ID_i and password pw_i . If the information matches with the data stored in the smart card, proceed to the next step, otherwise, reject.

Step 3-2. The smart card computes $D_i = T \cdot Reg_i$ and $V_i = T \cdot H(pw_i)$, where T is a current timestamp. The smart card picks a random integer k and computes: $\{C_1 = kP; C_2 = (D_i - V_i) + kP_{rs}\}$. After that, the terminal sends a login message $\{ID_i, C_1, C_2, T\}$ to the RS over a public channel.

Step 3-3. Receiving a login request at a timestamp T' , the RS verifies if $(T' - T) \geq \Delta T$, where ΔT denotes the expected valid time interval for transmission delay, then the RS rejects the login request.

Step 3-4. The RS checks if the following equation holds:

$$e(C_2 - sC_1, P) \stackrel{?}{=} e(H(ID_i), P_{rs})^T \quad (1)$$

If Eq. (1) holds, the RS accepts the login request, otherwise rejects.

Phase 4: Password Change

The user U_i can change password without assistance from the RS. He performs the following steps:

Step 4-1. The user U_i inputs his ID_i and the old password pw_i . The smart card checks validity by the equation:

$$e(Reg_i, P) = e(H(ID_i), P_{rs})e(H(pw_i), P) \quad (2)$$

If the equation holds, the smart card allows the user to change his password.

Step 4-2. The user inputs a new password pw_i^* .

Step 4-3. The smart card stored the new authentication information: $Reg_i^* = Reg_i - H(pw_i) + H(pw_i^*) = sH(ID_i) + H(pw_i^*)$

4. Weakness of Jia *et al.*'s scheme

Jia *et al.* [10] claimed that the remote user authentication scheme is secure against the forgery attack by using the ElGamal encryption to provide confidentiality to the registration information D_i and V_i . However, we show that their scheme could not sustain an impersonation attack. From eavesdropping on the login requests of a user, an attacker can produce a fake login request which helps the attacker bypass the authentication check of the RS as a legitimate user later. Our attack works as follows:

Assuming that an attacker succeeded to eavesdrop on a login request sent by the user U_i to the RS at time T_1 is $\{ID_i, C_1, C_2, T_1\}$. The attacker modifies the login request to the new one which can be used to login at time T_2 . He computes: $C'_1 = T_1^{-1}T_2C_1$ and $C'_2 = T_1^{-1}T_2C_2$. The new login request $\{ID_i, C'_1, C'_2, T_2\}$ can pass the verification, Eq. (1), of the RS as shown below:

$$\begin{aligned} e(C'_2 - sC'_1, P) &= e(T_1^{-1}T_2C_2 - T_1^{-1}T_2sC_1, P) = \\ &= e(T_1^{-1}T_2(C_2 - sC_1), P) \\ &= e(T_1^{-1}T_2(D_i - V_i + kP_{rs} - skP), P) \\ &= e(T_1^{-1}T_2(D_i - V_i), P) \\ &= e(T_1^{-1}T_2(T_1(Reg_i - H(pw_i))), P) \\ &= e(T_2((Reg_i - H(pw_i))), P) \\ &= e(T_2((sH(ID_i) + H(pw_i) - H(pw_i))), P) \\ &= e(T_2sH(ID_i), P) = e(H(ID_i), P_{rs})^{T_2} \end{aligned}$$

By intercepting the communication line, the attacker sends this new login message and, authenticates successfully with the RS and uses service freely.

5. Our Improvement Scheme

The problem of Jia *et al.* [10] scheme is that they did not guaranty the integrity of the login message, thus, an attacker just modifies an eavesdropped login message and can impersonate a legitimate user successfully. We present an improvement scheme which overcomes this problem.

The setup and registration phases are the same as Jia *et al.*'s scheme except that in the registration phase, the RS employs an additional operation, a hash function $h : \{0, 1\}^* \rightarrow Z_q^*$, into the smart card. The authentication phase is described as follows:

Phase 3: Authentication

As in the original scheme, the user first passes the smart card's identification then sends a login request to the RS. The RS checks the login request to verify if that user is legitimate or not. The user U_i logs in by the following steps:

Step 3-1. U_i inserts the smart card into the input device and enters his identity ID_i and password pw_i . The smart card ensures this is an actual user by checking the equation:

$$e(Reg_i - H(pw_i), P) = e(H(ID_i), P_{rs}) \quad (3)$$

If the equation holds, U_i is a legitimate user and the smart card goes to the next step, otherwise, it cancels.

Step 3-2. The smart card selects a random integer k and performs calculation: $C_1 = kP$, $C_2 = h(C_1, T)(Reg_i - H(pw_i) + kP_{rs})$. Here, T is the timestamp at the computation. After that, the terminal sends a login message $\{ID_i, C_1, C_2, T\}$ to the RS over a public channel.

Step 3-3. Receiving a login request at a timestamp T' , the RS verifies if $(T' - T) \geq \Delta T$, where ΔT is the expected valid transmission delay interval, then the RS rejects the login request. Otherwise, the RS proceeds the next step.

Step 3-4. The RS checks the following equation:

$$e(C_2 - sC_1, P) = e(h(C_1, T)H(ID_i), P_{rs}) \quad (4)$$

If Eq. (4) holds, the login is accepted, otherwise rejected. The correctness of Eq. (4) can be checked easily:

$$\begin{aligned} & e(C_2 - sC_1, P) \\ &= e(h(C_1, T)(Reg_i - H(pw_i) + kP_{rs}) - skP, P) \\ &= e(h(C_1, T)(Reg_i - H(pw_i)), P) \\ &= e(h(C_1, T)(sH(ID_i) + H(pw_i) - H(pw_i)), P) \\ &= e(h(C_1, T)sH(ID_i), P) \\ &= e(h(C_1, T)H(ID_i), sP) \\ &= e(h(C_1, T)H(ID_i), P_{rs}) \end{aligned}$$

Phase 4: Password Change

The steps to change password are the same as the original scheme except how the user identifies himself to the smart card. The smart card will validate the user by checking Eq. (3) instead of Eq. (2). Other steps keep unchanged.

Remarks: For simpler implementation to the smart card, we can adopt an exclusive OR, \oplus , instead of using the hash function h . Utilizing \oplus operation in the scheme

will minimize the change in the smart card implementation. Usually, this is a basic operation having very low computational complexity. In this case, the only quantity $h(C_1, T)$ will be changed to $C_{1(x)} \oplus T$, where $C_{1(x)}$ is x -coordinate of the C_1 . The remaining part of the scheme is unchanged. The security of the scheme is maintained.

6. Discussion

6.1. Security Analysis

In our improvement scheme, the replaying attack can be avoided due to using a timestamp technique as in the original scheme. Given that the adversary recorded a login message $\{ID_i, C_1, C_2, T\}$, if he wants to authenticate at the later time, he needs to recompute values C_1 and C_2 to pass the verification in Eq. (4). This cannot be done without knowing the secret value Reg_i , pw_i , and k simultaneously.

For the impersonation attack, one can consider $\{C_1, C_2\}$ is a signature on the timestamp value T with randomness C_1 embedded. Hence, if an adversary forges these values successfully, it can be shown that there exists an algorithm can break the CDH problem in the group G_1 .

Theorem 1. *If an adversary can perform an impersonation attack on the authentication scheme, there exists an algorithm can break the CDH problem in the group G_1 .*

Proof (Sketch): We use the same proving technique in [14]. Suppose that there exists an adversary \mathcal{A} performs the impersonation attack successfully on the authentication scheme for a given ID within a time bound t with the probability ϵ . \mathcal{A} can query h , H , and user authentication for at most q_h , q_H and q_P times, respectively. Assume that $\epsilon \geq 10(q_P + 1)(q_h + q_P)/q$. We can construct an algorithm \mathcal{B} which breaks the CDH problem (P, aP, bP) in G_1 as follows: The algorithm \mathcal{B} sets $P_{rs} = aP$. For any identity ID_i other than the identity of the impersonated user ID , output the hash query $H(ID_i) = x_iP$ for $x_i \in_R Z_q^*$. If $ID_i = ID$, set $H(ID_i) = bP$. The output of the query to $h(\cdot, \cdot)$, h_j where $j = 1, 2, \dots, q_P$, is chosen randomly from Z_q^* . At the registration phase, the algorithm \mathcal{B} also can answer the registration request from \mathcal{A} by returning $Reg_i = x_iP_{rs} + H(pw_i)$, where pw_i is given by \mathcal{A} and $H(pw_i)$ can be chosen randomly from the group G_1 . \mathcal{A} is not allowed to ask this type of queries for $ID_i = ID$.

\mathcal{B} also provides login requests $\{ID_{i_j}, C_{1i_j}, C_{2i_j}, T_{i_j}\}$ to \mathcal{A} for verification. \mathcal{B} selects $r_j \in_R Z_q^*$ and computes the login request $\{ID_{i_j}, C_{1i_j}, C_{2i_j}, T_{i_j}\}$ as follows:

$$C_{1i_j} = r_jP - h_jH(ID_{i_j}) \text{ and } C_{2i_j} = r_jP_{rs}$$

\mathcal{A} verifies the correctness of the login request by the following equation which is equivalent to Eq. (4):

$$e(C_{2i_j}, P) = e(C_{1i_j} + h(C_{1i_j}, T_{i_j})H(ID_{i_j}), P_{rs}) \quad (5)$$

Later, \mathcal{A} outputs a valid login request for the user ID as $\{ID, C_1, C_2, T\}$. By replaying \mathcal{A} with the same random tape but a different hash function h' and using the forking lemma in [12], \mathcal{B} comes up with two different login requests $\{ID, C_1, C_2, T\}$ and $\{ID, C_1, C'_2, T\}$ such that $h'(C_1, T) \neq h(C_1, T)$, hence $C_2 \neq C'_2$, with probability $\geq 1/9$. Finally, \mathcal{B} obtains abP from

$$abP = \frac{C'_2 - C_2}{h'(C_1, T) - h(C_1, T)}$$

The total running time t' of \mathcal{B} is bounded by $23q_h t/\epsilon$ as per the forking lemma [12]. \square

Regarding the password change capability, users perform changing their password without intervention of the RS. Moreover, this will prevent a malicious RS from using their identities information illegally. The risk of the storing password also is avoided.

6.2. Performance

In Table 1, H and h are hash operations, P is pairing computation, A and S are elliptic curve point addition and scalar multiplication, respectively. E is exponentiation of pairing value.

Phases	Improvement	Jia <i>et al.</i> [10]
Reg.	2H + S	2H + S
Login	A + 3S + H + h	A + 4S + H
Verfy.	2S + A + 2P + H + h	S + A + E + 2P + H
Pwd.Chg.	A + 2P	3P

Table 1. Computational Complexity.

Our improvement does not degrade the performance of the original scheme. In fact, by changing the calculation slightly, our scheme is more efficient than the original scheme. In the original scheme, to validate a user, the smart card has to evaluate Eq. (2), consuming 3 pairing operations. In our scheme, this verification is done by Eq. (3) which has only 2 pairing operations. The additional point adding operation in this equation is much cheaper than 1 pairing operation. The similarity is done in the computation of C_1 and C_2 , saving 1 scalar multiplication. The detailed comparison is given in Table 1.

7. Concluding Remarks

In this paper, we reviewed the authentication scheme using bilinear pairings proposed by Jia *et al.* and showed a proper impersonation attack on this scheme. Fortunately,

we are able to fix the scheme and provide an improvement scheme with provable security. The new authentication scheme is more secure as well as more efficient than the original scheme. For further work, we consider to develop a new authentication scheme which is supporting mutual authentication for preventing malicious remote servers from deriving information of registered users to use illegally.

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