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# 익명성을 제공하는 신원 기반 그룹 키 합의 프로토콜에 대한 연구

A Study on Identity-based Group Key Agreement Schemes with Anonymity



박 혜 원 (朴 惠 媛 Park, Hye-won) 정보통신공학과

Department of Information and Communications Engineering

한국과학기술원

Korea Advanced Institute of Science and Technology

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# A Study on Identity-based Group Key Agreement Schemes with Anonymity

Advisor: Professor Kwangjo Kim

by

#### Park, Hye-won

Department of Information and Communications Engineering Korea Advanced Institute of Science and Technology

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Professor Kwangjo Kim

Professor Kwangjo Kim Advisor

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# 박혜 원

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심사위원장 김 광 조 (인)

심사위원 이 영 희 (인)

심사위원 염 용 진 (인)

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#### Abstract

ID-based group key agreement (GKA) has been increasingly researched with the advantage of simple public key management. However, identities of group members can be exposed in this protocol, so eavesdroppers can easily learn the information of the group members. Recently, Wan et al. [11] proposed a solution for this problem, an anonymous ID-based GKA protocol, which can keep group members' anonymity to outside eavesdroppers; nevertheless, the protocol has some security flaws.

This paper shows that Wan et al.'s GKA is insecure against colluding attack and their joining/leaving protocols do not guarantee forward and backward secrecy. We also propose a new forward secure ID-based GKA with anonymity from enhancing Wan et al.'s joining/leaving protocols. In our scheme, i) impersonation by colluding attack cannot be done because ID-based signature is used, ii) joining or leaving members cannot obtain the previous or later session group key using the previous individual secrets, so group forward and backward secrecy are provided. Moreover, our protocols can operate efficiently compared with the previous ID-based GKA protocols.

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# Contents

	Abs	tract	i
	Con	tents	iii
	List	of Tables	v
	List	of Figures	vi
1	Inti	roduction	1
	1.1	Overview	1
	1.2	Our Contribution	2
	1.3	Organization	2
2	Pre	eliminaries	4
	2.1	Security Requirements for GKA protocol	4
	2.2	Bilinear Map	5
	2.3	ID-based Cryptosystem Setup	5
	2.4	Adversarial Model	5
3	ID-	based GKA and Its Analysis	7
	3.1	Choi, Hwang, and Lee	7
	3.2	Kim, Kim, Ha, and Yoo	8
	3.3	Zhou, Susilo, and Mu	9
	3.4	Yao, Wang, and Jiang	11
	3.5	Park, Asano, and Kim	12
4	Rev	view on [WRLP08] Protocols	14
	4.1	Notations	14
	4.2	[WRLP08-GKA]	14
	4.3	[WRLP08-Join]	15
	4.4	[WRLP08-Leave]	16
5	For	ward Secure ID-based GKA Protocol with Anonymity	17
	5.1	Security Weaknesses on [WRLP08]	17
		5.1.1 Impersonation by Colluding Attack in [WRLP08-GKA] Protocol	17

Re	efere	ences			30
Sı	ımm	ary (i	n Korean)		29
7	Cor	nclusio	on		28
	6.2	Perfor	mance		25
	6.1	Securi	ty		22
6	Ana	alysis			22
		5.2.2	Leaving Protocol		21
		5.2.1	Joining Protocol		20
	5.2	Our p	rotocols		19
		5.1.3	Weakness on Forward Secrecy in the [WRLP08-Leave] Protocol $ . $ .		19
		5.1.2	Weakness on Backward Secrecy in the [WRLP08-Join] Protocol	•	18



# List of Tables

6.1	Security Requirements	$2^{2}$
6.2	Computational overhead	20
6.3	Computational overhead in joining	27
6.4	Computational overhead in leaving	27



# List of Figures

1 ID-based cryptosystem		:
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#### 1. Introduction

#### 1.1 Overview

In modern society, many group-oriented applications exist, such as Internet conferencing, chatting, or collaborative workspace. These applications usually require privacy and integrity for communication messages; that is, all the messages exchanged during communication should be protected from eavesdroppers. For this reason, the group members need a common secret key to encrypt their communication messages. Group key agreement (GKA) is the protocol that the legitimated group members share a common secret group key.

In the technical report of Manulis [7], the author defines GKA as follows.

A group key agreement protocol or mechanism is a group key establishment technique in which a shared secret is derived by two or more parties as a function of the information contributed by, or associated with, each of these (ideally) such that no party can predetermine the resulting value.

Every collaborative and distributed systems can use GKA for the secure communication. With the established key, the group members can protect their communication messages from attackers using symmetric encryption. In addition, an authenticated GKA provides mutual key authentication during GKA.

After Shamir proposed ID-based cryptosystem [1], ID-based GKA protocols [4, 6, 8, 10, 12] have been increasingly researched with the advantage of simple public key management. Figure 1.1 shows the flow of ID-based cryptosystem. In ID-based cryptosystem, a user's identity information, e.g. email adderess or PIN number, is used as public keys, and a key generation center (KGC) generates the corresponding private keys; hence, any certificate is not required to bind user names with their public keys. Though ID-based GKA protocols have the advantage, it has one serious problem that anonymity of group members cannot be guaranteed. The identities of group members always can be exposed to eavesdroppers during the protocol execution.

In 2008, Wan et al.[11] proposed an anonymous ID-based GKA protocol. Their protocol keeps the advantage of the ID-based cryptosystem, and guarantees anonymity of the

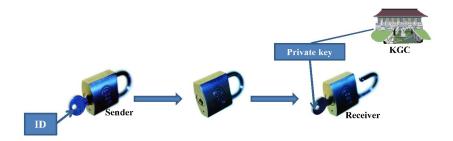


Figure 1.1: ID-based cryptosystem

identities of the current group members that eavesdroppers cannot get any information about the members. The authors also proposed joining and leaving protocols for dynamic operation of a single user.

#### 1.2 Our Contribution

In this paper, we show that Wan et al.'s GKA protocol is insecure in the presence of malicious participants. Two malicious neighbors of a specific user, who can collude with the group initiator, can impersonate the user during the group execution. In addition, their joining protocol cannot provide group backward secrecy, so joining members can get the group key of the previous session; similarly, the leaving protocol cannot provide group forward secrecy so that leaving members can get the later session key. We present the security flaws of these protocols, and propose our enhanced joining/leaving protocols. In our protocols, i) ID-based signature is used, so impersonation by colluding attack cannot be done, ii) because all the group members have to compute individual secrets for each session to generate a new session group key, no joining or leaving member can obtain the previous or later session group key using the previous individual secrets; i.e., our protocols can provide group forward/backward secrecy, and prevent impersonation by colluding attack. Moreover, our protocols can operate efficiently compared with the previous ID-based GKA protocols.

## 1.3 Organization

The rest of our paper is organized as follows: Chapter 2 explains preliminaries, such as security requirements for GKA, bilinear map, ID-based cryptosystem setup, and adversar-

ial model. In Chapter 3, we review previous ID-based GKA protocols and analyze them. The review on Wan *et al.*'s protocols, which we focused on, is described in Chapter 4. Chapter 5 shows weaknesses of Wan *et al.*'s protocols and our improved joining and leaving protocols. Analysis of our protocols are given in Chapter 6. Finally, we summarize and conclude our paper in Chapter 7.



#### 2. Preliminaries

#### 2.1 Security Requirements for GKA protocol

Security of GKA protocol can be defined with the definition of adversaries who want to break or interrupt the protocol. The passive adversary only eavesdrops, does not modify, the communication between group participants during GKA. The active adversary can control the communication; namely, it can modify the communication messages or impersonate the group participants. Because all GKA protocols are exposed to passive or active adversaries, we have to consider the requirements for GKA protocols to protect the identities or the communication messages of group members from those adversaries. In case of anonymous ID-based GKA protocol, it becomes more complicated that anonymity and unlinkability should be provided. Wan et al. defined the security requirements for their anonymous ID-based GKA protocol. Additionally, we consider one more requirement, entity authentication, because each legitimated group member should have confidence that the other members are really participating in the protocol while the protocol provides anonymity. The following terms are the description of the security requirements against all types of adversaries:

- Anonymity: The communication messages do not carry any information about group members' identities for protecting the identities from the outside eavesdropper.
- Unlinkability: The group members' activities in two different sessions must be independent; in other words, all the sessions are unlinkable to each other.
- Group Key Secrecy: Any adversary cannot compute the session group key.
- Group Forward Secrecy: Any adversary (especially the leaving member) who knows
  the previous group key cannot obtain the subsequent group key and communication
  messages.
- Group Backward Secrecy: Any adversary (especially the joining member) who knows
  the current group key cannot obtain the preceding group key and communication
  messages.

- Perfect Forward Secrecy: Revealing the long-term secret key does not affect the secrecy of the established session keys from previous protocol sessions.
- Entity Authentication: Each group member should have confidence that the other members are actually involved in the protocol.

#### 2.2 Bilinear Map

 $G_1$  is an cyclic additive group, and  $G_2$  is a cyclic multiplicative group with same order q. Assume that discrete logarithm problem (DLP) is hard in both  $G_1$  and  $G_2$ . A mapping  $e: G_1 \times G_1 \to G_2$  which satisfies the following properties is called a bilinear map from a cryptographic point of view:

1. Bilinearity:  $e(aP,bQ) = e(P,Q)^{ab}$  for all  $P,Q \in G_1$  and  $a,b \in Z_q^*$ .

$$e(P_1, Q)e(P_2, Q) = e(P_1 + P_2, Q)$$

$$e(P,Q_1)e(P,Q_2) = e(P,Q_1 + Q_2)$$

2. Non-degeneracy: If a generator  $P \in G_1$  then e(P, P) is a generator of  $G_2$ ; in other words,  $e(P, P) \neq 1$ .

## 2.3 ID-based Cryptosystem Setup

Many ID-based GKA protocols are based on Boneh and Franklin's ID-based cryptosystem setup [2] using bilinear pairing. To start setup phase, a trusted KGC chooses a random  $s \in \mathbb{Z}_q^*$  as the master secret key,  $P_{pub} = sP$  as the public key, and generates the system parameters:

$$param = \langle G_1, G_2, q, e, P, P_{pub}, H_1 \rangle,$$

where P is an arbitrary generator of  $G_1$ , and  $H_1$  is a hash function,  $H_1: \{0,1\}^* \to Z_q^*$ .

Then KGC produces the public key  $Q_{ID} = H_1(ID)$  and the private key  $S_{ID} = sQ_{ID}$  using the user's identity ID. For instance, a user with identity  $U_i$  has the static key pair  $\langle Q_i, S_i \rangle$ .

#### 2.4 Adversarial Model

As explained in Section 2.1, there are two types of adversaries: passive and active adversaries. The ability of the passive adversary is restricted to eavesdropping communications

only, but the *active adversary* additionally can replace, modify, or intercept messages. The goals of adversaries in GKA protocols are computing the subset of group keys or impersonation of the legitimate group member.

To provide computational security, we introduce two computationally infeasible problems, Bilinear Diffie-Hellman (BDH) and Elliptic Curve Diffie-Hellman (ECDH) problems.

- BDH Problem: Given P, aP, bP, and cP, compute  $e(P, P)^{abc}$  where  $P \in G_1$ ,  $a, b, c \in \mathbb{Z}_q^*$ , and e is a bilinear pairing.
- ECDH Problem: Given P, aP, and bP, compute abP where P is an element of an elliptic curve and  $a, b \in \mathbb{Z}_q^*$

BDH/ECDH assumptions mean that BDH/ECDH problems are hard to solve in a polynomial time with non-negligible probability.



# 3. ID-based GKA and Its Analysis

In this Chapter, we review previously proposed ID-based GKA protocols. We also analyze security weaknesses and performance of those protocols.

#### 3.1 Choi, Hwang, and Lee

Choi et al.([CHL04]) [4] proposed two-round ID-based GKA protocol in 2004. The protocol proceeding is as follows:

**Round 1.**  $U_i$  selects random  $a_i \in \mathbb{Z}_q^*$ , and broadcasts

$$< P_i = a_i P, T_i = a_i P_{pub} + h_i S_i >,$$
  
where  $h_i = H(P_i)$ .

**Round 2.** After receiving  $\langle P_i, T_i \rangle$  pairs,  $U_i$  verifies

$$e(\sum_{k \in \{-1,1,2\}} T_k, P) = e(\sum_{k \in \{-1,1,2\}} (P_k + h_k Q_k), P_{pub})$$

If verified,  $U_i$  broadcasts

$$D_i = e(a_i(P_{i+2} - P_{i-1}), P_{i+1}).$$

**Key Computation.**  $U_i$  computes the session key,

$$K_i = e(a_i P_{i-1}, P_{i+1})^n D_i^{n-1} D_{i+1}^{n-2} \dots D_{i-2}.$$

After proceeding the protocol, all the group members compute one common shared key K, where  $K = K_i = e(P, P)^{a_1 a_2 a_3 + ... + a_{n-1} a_n a_1 + a_n a_1 a_2}$ .

This protocol provides security proof under Decisional Hash Bilinear Diffie-Hellman (DHBDH) assumption. However, it only adapts partial authentication because the user authentication verifies only three  $\langle P_i, T_i \rangle$  pairs of  $U_{i-1}$ ,  $U_{i+1}$  and  $U_{i+2}$ . Zhang and Chen [3] showed that the impersonation attack on the protocol is possible when two malicious users get and replay the previous authentication transcripts of the entity, and suggested using time parameter to prevent this attack. In 2007, Shim [9] showed that three malicious users,  $U_{i-2}, U_{i-1}$ , and  $U_{i+1}$ , can collude and impersonate  $U_i$  without replaying

the previous transcripts. To prevent this attack, she suggested that each user should authenticate all participating entities for each round.

In 2008, Choi et al.([CHL08]) [10] proposed an improved GKA protocol from [CHL04] protocol. They proved that Shim's solution is not enough because insider attack is still possible in [CHL04] protocol. In [CHL08] protocol, the concatenation of all ID and  $P_i$  are attached to  $D_i$ , and verified by all users. The batch verification is used for reducing the verification time.

Setup 
$$PID = ID_1 || ... || ID_n$$

**Round 1.**  $U_i$  selects random  $a_i \in \mathbb{Z}_q^*$ , and broadcasts

$$< P_i = a_i P, T_i = a_i P_{pub} + h_i S_i >,$$
  
where  $h_i = H(P_i || PID).$ 

**Round 2.** After receiving  $\langle P_i, T_i \rangle$ , pairs,  $U_i$  verifies

$$\begin{split} e(\sum_{k \in \{-1,1,2\}} T_k, P) &= e(\sum_{k \in \{-1,1,2\}} (P_k + h_k Q_k), P_{pub}) \\ \text{If verified, } U_i \text{ makes signature pair } (W_i, V_i) \text{ on a message } D_i ||SID||PID, \\ \text{where } SID &= P_1 ||...||P_n, \\ \text{and broadcasts } ID_i || &< D_i, (W_i, V_i) >. \\ D_i &= e(a_i(P_{i+2} - P_{i-1}), P_{i+1}). \end{split}$$

**Key Computation.** If the verification of all  $(W_i, V_i)$  is verified,  $U_i$  computes the session key,

$$K_i = e(a_i P_{i-1}, P_{i+1})^n D_i^{n-1} D_{i+1}^{n-2} \dots D_{i-2}.$$

Because the probability that the PIDs and SIDs are different in each session is high, the transcript cannot be replayed or impersonated. This GKA protocol requires 6 pairing computations per user, so two more pairing computations are used for additional verification.

#### 3.2 Kim, Kim, Ha, and Yoo

In [6], Kim et al. ([KKHY04]) proposed an ID-based GKA protocol which requires only one communication round.

**Round 1.**  $U_i$  select random  $a, a_i \in \mathbb{Z}_q^*$ , then broadcasts

$$\langle a_i P_{pub}, P_i = aP, T_i = aa_i P_{pub} + H(P_i, a_i P_{pub})S_i \rangle$$
.

Key Computation.  $U_i$  verifies

$$e(T_j, P) = e(H(P_j, a_j P_{pub}) Q_j, P_{pub}) \cdot e(a_j P_{pub}, P_j).$$

Then  $U_i$  computes the session key,

$$K_i = e(Q_1, a_1 P_{pub}) \cdot ... \cdot e(a_i S_i, P) \cdot ... \cdot e(Q_n, a_n P_{pub}) K_s = H_2(K_i)$$

Although the protocol is efficient in communication time, each user must compute 4n-3 pairing computations: 3(n-1) times for verifying the other users, and n times for generating session group key. Moreover, the protocol suffer from replay attack or revealing session group key. The replay attack is possible if malicious user use the previous transcript  $\langle a_i P_{pub}, (P_i, T_i) \rangle$  to impersonate  $U_i$  in another group because the protocol does not have time stamp and the verification only check the validity of the message. The other users cannot know whether the message is reused or not. In key generation step, the equation for computing session key can be expressed as follows:

$$K_{i} = e(Q_{1}, a_{1}P_{pub}) \cdot \dots \cdot e(a_{i}S_{i}, P) \cdot \dots \cdot e(Q_{n}, a_{n}P_{pub})$$

$$= e(Q_{1}, a_{1}P_{pub}) \cdot \dots \cdot e(a_{i}Q_{i}, P_{pub}) \cdot \dots \cdot e(Q_{n}, a_{n}P_{pub})$$

$$= e(Q_{1}, a_{1}P_{pub}) \cdot \dots \cdot e(Q_{i}, a_{i}P_{pub}) \cdot \dots \cdot e(Q_{n}, a_{n}P_{pub})$$

Because the communication messages are exchanged through the broadcast channel, any eavesdropper can easily get the message  $\langle a_i P_{pub}, (P_i, T_i) \rangle$ . The above equation can be computed with  $Q_i$  and  $a_i P_{pub}$ . For this reason, impersonation using the previous transcript and revealing session group key are possible in [KKHY04] protocol.

## 3.3 Zhou, Susilo, and Mu

Zhou et al. [8] proposed two ID-based GKA protocols: one has one communication round ([ZSM06]-1), and the other has two rounds([ZSM06]-2). [ZSM06]-1 protocol proceeding is as follows:

Round 1. 
$$U_i$$
 picks  $\delta \leftarrow G_2$ ,  $r, k_1 \leftarrow \{0, 1\}^n$   
Then computes  $P_i^j$   
 $P_i^j = r_i \bigoplus H_2(e(S_i, Q_j) \cdot \delta_i)$  where  $1 \leq j \leq n$  and  $j \neq i$   
Computes & broadcasts  $D_i$ 

$$D_i = \langle \delta, P_i^1, ..., P_i^{i-1}, P_i^{i+1}, ..., P_i^n, H_3(r_i) \cdot k_i, L \rangle$$

**Key Computation.**  $U_i$  computes

$$k'_j = H_3(H_2(e(Q_j, S_i) \cdot \delta_j) \odot P_j^i) \odot V_j$$

Session Key  $K = K_i = k'_1 \odot ... \odot k'_n$ 

[ZSM06]-1 protocol is efficient in communication because each user broadcasts only once during GKA, but computation cost is comparatively large that each user is required to compute 2(n-1) pairing computations, and the message size for broadcasting is n+2 for each user.

Following is [ZSM06]-2 protocol proceeding:

**Round 1.** Initiator  $U_1$ : Picks  $\delta \leftarrow G_2$ ,  $r, k_1 \leftarrow \{0,1\}^n$ 

Then computes

$$P_i = r \bigoplus H_4(e(S_1, Q_i) \cdot \delta) \ (1 \le i \le n)$$

Computes & broadcasts  $D_1$ 

$$D_1 = \langle \delta, P_2, ..., P_n, X_1 = H_5(r) \cdot k_1 P, Y_1 = k_1 P_{pub}, L \rangle$$

**Round 2.**  $U_i(2 \le i \le n)$ : Finds appropriate  $P_i$  from  $D_1$ .

Then computes  $r' = H_4(e(S_i, Q_1) \cdot \delta) \bigoplus P_i = r$ 

Random  $k_i \leftarrow Z_P^*$ 

Computes & Broadcasts  $D_i$ 

$$D_i = \langle X_i, Y_i \rangle = \langle H_5(r) \cdot k_i P, k_i P_{pub} \rangle$$

Key Computation. All user compute

$$z_i = H_5(r)^{-1} \cdot X_i \ (1 \le i \le n),$$

then verify the following equation.

$$e(P, \sum_{j=1}^{n} Y_j) = e(P_{pub}, \sum_{j=1}^{n} z_j)$$

**Session Key** 
$$K = K_i = H_6(z_1) \bigoplus ... \bigoplus H_6(z_n)$$

[ZSM06]-2 protocol has one more communication round but much less computation cost than [ZSM06]-1 protocol that two-round protocol uses the batch verification for reducing the verification cost. However, in [ZSM06]-2 protocol, the existence of malicious participants is not considered. Also, the verification only executes if the message is correctly generated with secret value r, not if the message is sent by correct user. Therefore, the malicious insider, who knows the secret value r, can impersonate the other users;i.e., impersonation attack by the insider will happen. In our previous paper [13], we showed

this impersonation attack. The following is an attack on the protocol that the legitimated user  $U_k$  impersonates the user  $U_i$ :

**Round 2.** Malicious insider  $U_m(i \neq m)$ :

Inject the message which is sent to  $U_i$ .

Find appropriate  $P_m$  from  $D_1$ .

Compute  $r' = H_4(e(S_m, Q_1) \cdot \delta) \bigoplus P_m = r$ 

Random  $k_i \leftarrow Z_P^*, k_m \leftarrow Z_P^*$ 

Compute & broadcast  $D_i$ ,  $D_m$ 

$$D_i = \langle X_i, Y_i \rangle = \langle H_5(r) \cdot k_i P, k_i P_{pub} \rangle$$

$$D_m = \langle X_m, Y_m \rangle = \langle H_5(r) \cdot k_m P, k_m P_{pub} \rangle$$

**Key Computation.** All users succeed to verify  $D_i$ 

$$e(P,\sum_{j=1}^n Y_j) = e(P_{pub},\sum_{j=1}^n z_j)$$

**Session Key** 
$$K = K_i = H_6(z_1) \bigoplus ... \bigoplus H_6(z_n)$$

In round 2 of the protocol, malicious user  $U_m$  can compute  $\langle X_i, Y_i \rangle$  pair using r because the computation does not need any private information of  $U_i$ . Then all the other users believe that they agreed session group key with legitimate user  $U_i$  even though  $U_i$  does not exist. This attack can also occur with colluding of several malicious users.

## 3.4 Yao, Wang, and Jiang

A 3-round ID-based GKA protocol was proposed by Yao *et al.* ([YWJ08])[12] in 2008. The first round is for identity authentication, the second is for key agreement, and the last round is for key confirmation.

**Round 1.**  $U_i$  selects random  $a_i \in Z_q^*$ , and then broadcasts

$$< P_i = a_i P, V_i = a_i P_{pub} + h_i S_i >,$$

where 
$$h_i = H(U, e(P_i, P_{pub}))$$
.

**Round 2.** After receiving  $\langle P_i, T_i \rangle$ , pairs,  $U_i$  verifies

$$e(\sum_{j \neq i} V_j, P) = e(\sum_{j \neq i} (P_j + h_j Q_j), P_{pub})$$

If verified,  $U_i$  computes

$$T = H_0(ID_1||P_1||...||ID_n||P_n)$$

and broadcasts

$$< X_i = a_i(P_{i+1} - P_{i-1} + T), Y_i = a_i T >.$$

**Round 3.** After receiving  $\langle X, Y \rangle$ , pairs,  $U_i$  verifies

$$e(\sum_{j\neq i} Y_j, P) = e(\sum_{j\neq i} P_j, T)$$

If verified,  $U_i$  computes

$$Z_i = e(na_i P_{i-1} + \sum_{j=0}^{n-1} (n-1-j)(X_{i+j} - Y_{i+j}), P_{pub})$$

and broadcasts

$$< C_i = H(i||U||P_1||...||P_n||X_1||...||X_n||Y_1||...||Y_n||Z_i>.$$

**Key Computation.** After check the validity of every  $C_j$   $(1 \le j \le n, j \ne i)$ ,

 $U_i$  computes the session key,

$$K_i = H(U||P_1||...||P_n||X_1||...||X_n||Y_1||...||Y_n||Z_i||C_1||...||C_n).$$

The protocol contains key confirmation step. However, the step is incomplete because it does not include users' private information, so attack on key confirmation is still possible. Moreover, the protocol requires O(n) pairing computations for each users.

## 3.5 Park, Asano, and Kim

We proposed the improved version ([PAK09])[13] of [ZSM06]-2 protocol. In [PAK09] protocol, equation of verification includes user's private key  $S_i$ , so malicious users cannot impersonate the  $U_i$  even though they get r.

**Round 1.** Initiator  $U_1$ :

Picks 
$$\delta, k_1 \leftarrow Z_q^*, \ r \leftarrow \{0,1\}^{|q|}$$

Computes 
$$P_i = r \bigoplus H_1(e(\delta S_1, Q_i)) \ (2 \le i \le n)$$

Computes & broadcasts  $D_1$ 

$$D_1 = \langle \delta, P_2, ..., P_n, X_1 = H_2(r||L)k_1P, Y_1 = k_1P_{pub} + H_2(r||L)S_1, L \rangle$$

**Round 2.**  $U_i(2 \le i \le n)$ :

Finds appropriate  $P_i$  from  $D_1$ .

Then computes 
$$r' = H_1(e(\delta S_i, Q_1)) \bigoplus P_i = r$$

Chooses  $k_i \leftarrow Z_q^*$  randomly. Computes & Broadcasts  $D_i$  $D_i = \langle X_i, Y_i \rangle$ 

$$D_i = \langle X_i, Y_i \rangle$$
  
=  $\langle H_2(r||L)k_iP, k_iP_{pub} + H_2(r||L)S_i \rangle$ 

Key Computation. Each user computes

$$z = H_2(r||L)^{-1} \cdot \sum_{i=1}^n X_i = \sum_{i=1}^n k_i P$$

Then verifies the following equation. If fails, then it halts.

$$e(P, \sum_{j=1}^{n} Y_j) = e(P_{pub}, z + H_2(r||L) \sum_{j=1}^{n} Q_j)$$

Session Key 
$$K = K_i = H_3(z)$$

In [PAK09] protocol, three points are improved from [ZSM06]-2 protocol. (i) We define  $\delta \leftarrow Z_q^*$  and change the encryption of secret value r in round 1 that  $\delta$  is multiplied to  $Q_1$  in  $G_1$  group. The multiplication in  $G_2$  group takes much more time than that in  $G_1$  group in practice, so we can reduce the time to encrypt r in our protocol. (ii) Multiplication of z is combined in our protocol to reduce the computation overhead. During key computation, we use hash function so key control of specific user is still impossible. (iii) The most important feature is that we modify the batch verification. In our protocol, each user broadcasts  $\langle H_2(r||L) \cdot k_i P, k_i P_{pub} + H_2(r||L) S_i \rangle$  to verify users. This computation includes the private key of each users, so malicious user cannot make this value arbitrary. The verification in our protocol can be done with the following equation.

$$\begin{split} e(P, \sum_{j=1}^{n} Y_j) \\ &= e(P, \sum_{j=1}^{n} (k_j P_{pub} + H_2(r||L) S_j)) \\ &= e(P, \sum_{j=1}^{n} (k_j s P) + \sum_{j=1}^{n} (H_2(r||L) s Q_j)) \\ &= e(P_{pub}, \sum_{j=1}^{n} (k_j P) + \sum_{j=1}^{n} (H_2(r||L) Q_j)) \\ &= e(P_{pub}, z + H_2(r||L) \sum_{j=1}^{n} (Q_j)) \end{split}$$

Nevertheless, [PAK09] protocol cannot guarantee the perfect forward secrecy. If all the previous transcripts and users' private keys are exposed, then the previous session key can be exposed.

## 4. Review on [WRLP08] Protocols

In this Chapter, we review Wan *et al.*'s anonymous ID-based GKA protocol ([WRLP08-GKA])[11] and joining([WRLP08-Join])/leaving([WRLP08-Leave]) protocols for single user operation in a specific group.

#### 4.1 Notations

The notations used in [WRLP08] protocol are as follows:

```
\begin{array}{lll} E_i(*) & \text{ID-based encryption using } U_i \\ E_K(*) & \text{Symmetric encryption using } K \\ Nym_i & \text{Pseudonym for } U_i \\ r_i & \text{Random number selected by } U_i \\ SIG_i & U_i\text{'s signature} \\ h & \text{A hash function } h: G_2 \times G_1 \rightarrow \{0,1\}^m \\ H & \text{A hash function } H: \{0,1\}^{m*n} \rightarrow \{0,1\}^k \text{ with a security parameter } k \\ \end{array}
```

## 4.2 [WRLP08-GKA]

There are n entities in [WRLP08-GKA] protocol: a group initiator  $U_1$  and the other group members  $U_2, ..., U_n$ . The initiator  $U_1$ , who knows all the identities of the other members, initiates a new session for starting the GKA protocol. The other members do not know the identities of the group members before the session starts. The protocol uses the public system parameter set param which is defined in Section 2.3.

1) Initiator  $U_1$  chooses pseudonyms for each user  $U_i$ .

$$U_1 \to U_i : E_i(U_1||...||U_n||Nym_1||...||Nym_n||SIG_1), r_1P$$

2)  $U_{i(\neq 1)}$  sends a message to  $U_{i-1}$  and  $U_{i+1}$ .

$$U_i \rightarrow U_{i+1}, U_{i-1} : Nym_i, r_iP$$

3)  $U_i$  verifies the pseudonyms, and computes

$$k_i = h(e(Q_{i+1}, S_i)||r_i r_{i+1} P)$$

$$k_{i-1} = h(e(Q_{i-1}, S_i) || r_i r_{i-1} P).$$
  
 $U_i \to *: Nym_i, X_i = k_i / k_{i-1}$ 

4)  $U_i$  verifies all the pseudonyms, and computes

$$k_{i+1} = k_i X_{i+1}, k_{i+2} = k_{i+1} X_{i+2}, \dots, k_{i+n-1} = k_{i+n-1} X_{i+n-1}.$$

**Session Key.** :  $K = H(k_1||k_2||..||k_n)$ 

After computing the session group key K,  $U_{i(\neq 1)}$  sends  $H(K||U_1||U_2||...||U_n)$  to  $U_1$ . Then  $U_1$  verifies whether all the other group members computed the same key or not.

#### 4.3 [WRLP08-Join]

In [WRLP08-Join] protocol,  $U_1$  firstly informs  $U_{n+1}$ 's joining. Then only  $U_1$  and  $U_n$ , who become  $U_{n+1}$ 's neighbors in the group, compute  $X'_1$  and  $X'_n$  to generate a new session group key. The protocol description is as follows:

1)  $U_1$  informs  $U_n$  and  $U_{n+1}$  about joining information.

$$\begin{split} U_1 &\to U_n: \ E_n(U_{n+1}||Nym_{n+1}||SIG_1) \\ U_1 &\to U_{n+1}: \ E_{n+1}(U_1||Nym_1||r_1P||U_n||Nym_n||r_nP||U_{n+1}||Nym_{n+1}||SIG_1) \end{split}$$

2)  $U_{n+1}$  computes

$$\begin{split} k_{n+1} &= h(e(Q_1, S_{n+1})||r_1r_{n+1}P)\\ k_n' &= h(e(Q_n, S_{n+1})||r_nr_{n+1}P).\\ X_{n+1} &= k_{n+1}/k_n'\\ U_{n+1} &\to U_1, U_n: Nym_{n+1}, \ r_{n+1}P, \ X_{n+1} \end{split}$$

**3)**  $U_1$  and  $U_n$  compute

$$U_1: k_{n+1} = h(e(Q_{n+1}, S_1)||r_1r_{n+1}P),$$

$$X'_1 = k_1/k_{n+1}$$

$$U_n: k'_n = h(e(Q_{n+1}, S_n)||r_nr_{n+1}P),$$

$$X'_n = k_n/k_{n-1}.$$

$$U_n \to U_1: X'_n$$

4)  $U_1$  informs all the members about changed information.

$$U_1 \to U_{n+1} : E_{n+1}(X_1'||X_2||...||X_{n-1}||X_n')$$
  

$$U_1 \to * : E_K(X_1'||X_{n+1}||X_n'||SIG_1)$$

New Session Key.  $K' = H(k_1||k_2||..||k'_n||k_{n+1})$ 

The group members, except  $U_1$  and  $U_n$ , do not need to compute  $X_i$  again during the joining protocol.

#### [WRLP08-Leave] 4.4

In [WRLP08-Leave] protocol,  $U_1$  informs  $U_l$ 's leaving. Then  $U_{l-1}$  and  $U_{l+1}$ , who were  $U_l$ 's neighbors in the previous session, compute  $X'_{l-1}$  and  $X'_{l+1}$  to generate a new session group key without  $U_l$ . The protocol description is as follows:

1)  $U_1$  informs  $U_{l-1}$  and  $U_{l+1}$  about leaving information.

$$U_1 \to U_{l-1}, U_{l+1} : E_K(U_l||Nym_l||U_{l-1}||Nym'_{l-1}||U_{l+1}||Nym'_{l+1}||SIG_1)$$

2)  $U_{l-1}$  and  $U_{l+1}$  exchange their new random values.

$$U_{l-1} \to U_{l+1} : Nym'_{l-1}, r_{l-1}P$$
  
 $U_{l+1} \to U_{l-1} : Nym'_{l+1}, r_{l+1}P$ 

3)  $U_{l-1}$  and  $U_{l+1}$  compute

$$\begin{aligned} u_{l-1} & \text{ and } U_{l+1} & \text{ compute} \\ U_{l-1} & : \ k'_{l-1} & = \ h(e(Q_{l+1}, S_{l-1})||r'_{l-1}r'_{l+1}P), \\ & X'_{l-1} & = \ k'_{l-1}/k_{l-2} \\ U_{l+1} & : \ k'_{l} & = \ h(e(Q_{l-1}, S_{l+1})||r'_{l-1}r'_{l+1}P), \\ & X'_{l+1} & = \ k_{l+1}/k'_{l-1}. \\ U_{l-1} & \to U_1 & : \ X'_{l-1} \\ U_{l+1} & \to U_1 & : \ X'_{l+1} \end{aligned}$$

4)  $U_1$  informs all the members about changed information.

$$U_1 \to * : E_K(U_l||U_{l-1}||U_{l+1}||X'_{l-1}||X'_{l+1}||SIG_1)$$

New Session Key.  $K' = H(k_1||...||k'_{l-1}||k_{l+1}||...||k_n)$ 

# 5. Forward Secure ID-based GKA Protocol with Anonymity

#### 5.1 Security Weaknesses on [WRLP08]

[WRLP08-GKA] protocol is insecure in the presence of malicious group participants. Moreover, [WRLP08-Join] and [WRLP08-Leave] protocols also have security weaknesses. In this Section, we show these weaknesses of the protocols.

# 5.1.1 Impersonation by Colluding Attack in [WRLP08-GKA] Protocol

To show an attack on [WRLP08-GKA] protocol, we assume that the malicious users  $U_{m-1}$  and  $U_{m+1}$  can collude with the group initiator  $U_1$  and want to impersonate the group member  $U_m$ . When starting the GKA protocol,  $U_1$  sends group information to the other group members except  $U_m$ , and sends one additional random value to  $U_{m-1}$  and  $U_{m+1}$ , who are two neighbors of  $U_m$ . Using this information,  $U_{m-1}$  and  $U_{m+1}$  can easily impersonate  $U_m$  without any private information of  $U_m$ . A detailed description of the attack is as follows:

1)  $U_1$  chooses pseudonyms for each user  $U_i$ .

$$U_1 \to U_{i(\neq m)}: E_i(U_1||...||U_n||Nym_1||...||Nym_n||SIG_1), r_1P$$
  
 $U_1 \to U_{m-1}, U_{m+1}: r_mP$ 

2)  $U_{m-1}$  and  $U_{m+1}$  get pseudonyms and send the random value only to  $U_{m-2}$  and  $U_{m+2}$ , while the other members send their random values to their two neighbors.

$$\begin{split} &U_{i} \to U_{i-1}, U_{i+1} \,:\, Nym_{i}, \; r_{i}P \\ &U_{m+1} \to U_{m+2}, \; (\text{not} \; U_{m}) \,:\, Nym_{m+1}, \; r_{m+1}P \\ &U_{m-1} \to U_{m-2}, \; (\text{not} \; U_{m}) \,:\, Nym_{m-1}, \; r_{m-1}P \end{split}$$

3)  $U_{m-1}$  and  $U_{m+1}$  can compute  $k_m$  and  $k_{m-1}$  which are originally generated by  $U_m$ .

$$U_{m+1}: k_m = h(e(Q_m, S_{m+1})||r_m r_{m+1}P)$$
  

$$U_{m-1}: k_{m-1} = h(e(Q_m, S_{m-1})||r_m r_{m-1}P).$$

$$U_{m+1}$$
 or  $U_{m-1} \to *: Nym_m, X_m = k_m/k_{m-1}$ 

4) If each  $U_i$  succeeds in verifying all the pseudonyms, then computes

$$k_{i+1} = k_i X_{i+1}, \ k_{i+2} = k_{i+1} X_{i+2}, \dots, \ k_{i+n-1} = k_{i+n-1} X_{i+n-1}.$$

**Session Key.**  $K = H(k_1||k_2||..||k_n)$ 

Through this attack, the other group members cannot recognize  $U_m$ 's missing, and just generate a session group key without  $U_m$ . This attack is possible because the security of messages depends on that of pseudonyms, and group members do not authenticate whether the message is actually generated by the specific member or not. Note that the computation of  $X_m$  can be computed by not only  $U_m$  but also  $U_{m-1}$  and  $U_{m+1}$ . Hence, malicious users,  $U_{m-1}$  and  $U_{m+1}$ , can impersonate the user  $U_m$ . To prevent this attack, each member should contain a signature while broadcasting  $X_i$ . If the members verify all the other members' signatures, they easily know  $U_m$ 's missing and stop the protocol. We recommend using Cheon et al.'s ID-based signature [5], which provides batch verification. With this scheme, users can reduce the authentication cost by verifying several signatures at once.

#### 5.1.2 Weakness on Backward Secrecy in the [WRLP08-Join] Protocol

We also prove that [WRLP08-Join] protocol cannot provide backward secrecy. In their joining protocol, we assume that joining member  $U_{n+1}$  can obtain the previous transcripts. Then  $U_{n+1}$  can compute not a new group key K' but the previous group key K, which is used before  $U_{n+1}$  joins the group.

During [WRLP08-Join] protocol execution,  $U_{n+1}$  computes a new session key K'. Equations for key generation in the GKA and joining protocols are as follows:

```
Previous session key: K = H(k_1||k_2||..||k_n)
New session key: K' = H(k_1||k_2||..||k_{n-1}||k'_n||k_{n+1})
```

In the new session group key, only  $k_n$  is changed from the previous session key, so  $U_{n+1}$  has all information about K, except  $k_n$ . If  $U_{n+1}$  can obtain  $k_n$ , then he also can compute the previous group key K. Here,  $U_{n+1}$  can extract  $k_n = k_{n-1}X_n$  using the previous transcript  $\langle Nym_n, X_n \rangle$  because it was broadcasted in the previous session. Therefore,  $U_{n+1}$  can compute the previous group key,  $K = H(k_1||k_2||...||k_n)$ .

Through this procedure, a joining member can compute the previous group key, using the previous transcript and the current session group key. Consequently, we can prove that [WRLP08-Join] protocol cannot guarantee backward secrecy.

#### 5.1.3 Weakness on Forward Secrecy in the [WRLP08-Leave] Protocol

Here we show that [WRLP08-Leave] protocol cannot provide forward secrecy. When  $U_l$  leaves the group, the other group members generate a new session group key K' with changed information. Equations for key generation in the GKA and leaving protocols are as follows:

```
Previous session key: K = H(k_1||k_2||..||k_n)
New session key: K' = H(k_1||...||k'_{l-1}||k_{l+1}||...||k_n)
```

Because only  $k_{l-1}$  is changed to  $k'_{l-1}$  in the new session group key,  $U_l$  has all information about K', except  $k'_{l-1}$ . If  $U_l$  can obtain  $k'_{l-1}$ , then he also can compute the new session group key K'. In the protocol, however,  $U_1$  informs all the members about changed information as follows:

$$U_1 \to *: E_K(U_l||U_{l-1}||U_{l+1}||X'_{l-1}||X'_{l+1}||SIG_1)$$

The message is encrypted using the previous group key K, so  $U_l$  can decrypt this message to get  $k'_{l-1} = k_{l-2}X'_{l-1}$ ; consequently, he can generate the new session key K'.

Through this procedure, a leaving member still can compute a new session group key although he no longer belongs to the group. Therefore, we can prove that [WRLP08-Leave] protocol cannot guarantee forward secrecy.

## 5.2 Our protocols

In the previous Section, we show the weaknesses on [WRLP08] protocol: impersonation by colluding attack, weaknesses on forward/backward secrecy in joining/leaving protocols. These weaknesses cause significant threats in group communication, so we propose our new joining/leaving protocols of [WRLP08] protocol to prevent the threats.

#### 5.2.1 Joining Protocol

In [WRLP08-Join] protocol, all the  $k_i$ 's except  $k_n$  are reused to generate a new session group key; accordingly, a joining member who obtain the previous transcript can compute the previous group key. To deal with this problem, all the  $k_i$ 's should be changed for each session, and the new group key should not contain information of the previous session. Computation of  $k_i$ , nevertheless, requires pairing computation which takes comparably high cost. Considering this fact, we design our joining protocol reducing the cost of computing  $k_i'$ . We define two hash functions  $g: \{0,1\}^m \to Z_q^*$ , and  $H_2: G_1 \to \{0,1\}^m$ .

1) Initiator  $U_1$  informs all the group members about  $U_{n+1}$ 's joining.

$$U_1 \to *: E_K(U_{n+1}||Nym'_1||...||Nym'_n||Nym_{n+1}||SIG_1)$$
  

$$U_1 \to U_{n+1}: E_{n+1}(U_1||...||U_n||U_{n+1}||Nym'_1||...||Nym'_n||Nym_{n+1}||r_1P||r_nP||SIG_1)$$

2)  $U_{n+1}$  computes

$$k_{n+1} = h(e(Q_1, S_{n+1})||r_1 r_{n+1} P)$$

$$k'_n = h(e(Q_n, S_{n+1})||r_n r_{n+1} P)$$

$$X_{n+1} = k_{n+1}/k'_n.$$

$$U_{n+1} \to U_1, U_n : Nym_{n+1}, r_{n+1} P, X_{n+1}$$

3)  $U_i$  computes

$$\begin{split} k_i' &= H_2(g(k_i)r_ir_{i+1}P), \ k_{i-1}' = H_2(g(k_i)r_ir_{i-1}P), \\ \text{and} \ U_1 \ \text{and} \ U_n \ \text{compute} \\ U_1 : \ k_{n+1} &= h(e(Q_{n+1},S_1)||r_1r_{n+1}P), \\ k_1' &= H_2(g(k_1)r_1r_2P) \\ U_n : \ k_n' &= h(e(Q_{n+1},S_n)||r_nr_{n+1}P), \\ k_{n-1}' &= H_2(g(k_n)r_nr_{n-1}P). \\ U_i &\to * : \ Nym_i', \ X_i' &= k_i'/k_{i-1}', \ SIG_i \end{split}$$

**Session Key.**  $K' = H(k'_1||k'_2||..||k'_n||k_{n+1})$ 

The  $k_i$ 's are changed in each session, so  $U_{n+1}$  cannot extract the previous session group key even if he has the previous transcripts. Additionally, all users contain their signatures when broadcasting  $X'_i$  to other users.

#### 5.2.2 Leaving Protocol

As in [WRLP08-Join] protocol, all the  $k_i$ 's except  $k_{l-1}$  are used to generate a new session group key in [WRLP08-Leave] protocol. Moreover, significant information to generate the new session group key is encrypted using the previous group key K, so leaving members can compute the new session group key K'. Two ways to solve this weakness are recomputing all the  $k_i$ 's and not using symmetric encryption, which uses the previous group key K as the symmetric key, for significant information. The protocol procedure is as follows:

1) Initiator  $U_1$  informs all the other members about  $U_l$ 's leaving.

$$U_1 \to * : E_K(U_l||Nym'_1||...||Nym'_n||SIG_1)$$

2)  $U_{l-1}$  and  $U_{l+1}$  exchange their new random values.

$$U_{l-1} \to U_{l+1} : Nym'_{l-1}, r_{l-1}P$$
  
 $U_{l+1} \to U_{l-1} : Nym'_{l+1}, r_{l+1}P$ 

3)  $U_i$  computes

$$k'_{i} = H_{2}(g(k_{i})r_{i}r_{i+1}P), \ k'_{i-1} = H_{2}(g(k_{i})r_{i}r_{i-1}P),$$
and  $U_{l-1}$  and  $U_{l+1}$  compute
$$U_{l-1} : \ k'_{l-1} = h(e(Q_{l+1}, S_{l-1})||r_{l-1}r_{l+1}P),$$

$$k'_{l-2} = H_{2}(g(k_{l-1})r_{l-1}r_{l-2}P)$$

$$U_{l+1} : \ k'_{l-1} = h(e(Q_{l-1}, S_{l+1})||r_{l-1}r_{l+1}P),$$

$$k'_{l+1} = H_{2}(g(k_{l+1})r_{l+1}r_{l+2}P).$$

$$U_{i} \to * : \ Nym'_{i}, \ X'_{i} = k'_{i}/k'_{i-1}, \ SIG_{i}$$
Session Key.  $K' = H(k'_{1}||...||k'_{i-1}||k'_{i+1}||...||k'_{n})$ 

The  $k_i$ 's are changed in each session, so  $U_l$  cannot compute the later session group key even if he has all the previous  $k_i$ 's. Also, the signature is included when each group member broadcasts  $X'_i$  to other users.

## 6. Analysis

In the previous Chapters, we recommended including signature during [WRLP08-GKA] protocol execution, and proposed our new joining/leaving protocols. Here, we analyze security and performance of our scheme in detail.

#### 6.1 Security

As already explained, there are two types of adversaries: passive and active adversaries. From eavesdropping the protocol execution, the passive adversary can get  $Nym_i$ ,  $r_iP$ , and  $X_i$  values. With this information, the adversary should not be able to get any information about the group members or the session group key. The active adversary want to interrupt the protocol execution or to impersonate the legitimate group member with more information than the passive adversary. This type of adversary additionally can obtain  $k_i$ 's or the public/private key pair  $\langle Q_i, S_i \rangle$  of the group member. In the case that the adversary gets the public/private key pair of the group member, he should not be able to compute the previous group keys. Also, the joining/leaving group member who gets the current or previous  $k_i$ 's should not be able to compute the precedeing/subsequent group keys.

a) Anonymity: In the GKA protocol, the message firstly sent from the initiator is encrypted using the private key of each member, and only the legitimate group members can decrypt this message and get the pseudonyms. Even though an outside eavesdropper obtains all the pseudonyms from the transcript, the eavesdropper cannot match them to the real identities of members unless he can decrypt the message using the private key.

Similarly, the informing messages sent from the initiator are encrypted using the group key of the previous session in the joining/leaving protocols.

```
Join : E_K(U_{n+1}||Nym'_1||...||Nym'_n||Nym_{n+1}||SIG_1)
Leave : E_K(U_l||Nym'_1||...||Nym'_n||SIG_1)
```

The eavesdropper cannot get the pseudonyms of all the group members without the previous session group key K. For this reason, the protocols keep the group members

anonymous to outside eavesdroppers.

- b) Unlinkability: When the session starts, the initiator always generates pseudonyms for the group members (also in the joining/leaving protocols); that is, the pseudonyms are never reused. Although the adversary wants to trace user information using all the pseudonyms of different sessions, he cannot link them to any user information because pseudonyms always change in each session and do not carry any information about the group members' identities.
- c) Group Key Secrecy: In the GKA protocol, the group key K is generated by concatenating all the  $k_i$ 's. Because the  $k_i$ 's are obtained sequentially with one  $k_i$  and all the other  $X_i$ 's, the adversary should have at least one  $k_i$  to compute the session group key. However, when computing  $k_i$ , it is difficult to compute  $r_i r_{i+1} P$  given  $\langle P, r_i P, r_{i+1} P \rangle$  tuple under the ECDH assumption; also computing  $e(Q_{i+1}, S_i)$  without the master secret key s is a hard problem under the BDH assumption. Consequently, the passive adversary cannot compute the group key K.
- d) Group Forward Secrecy: Our leaving protocol provides group forward secrecy when a user leaves the group; in other words, the  $U_l$  cannot compute the subsequent group key. In our protocol, all the  $k_i$ 's changes in each session and no symmetric encryption is used to encrypt new  $X_i$ 's, so  $U_l$  cannot extract  $k'_i$  using  $k_i$ . Also, under the ECDH assumption, it is hard to compute  $r_i r_{i+1} P$  given  $\langle P, r_i P, r_{i+1} P \rangle$  tuple when computing  $k'_i = H_2(g(k_i)r_ir_{i+1}P)$ ; therefore,  $U_l$  cannot compute  $k'_i$  although he has all the previous  $k_i$  and  $r_i P$ . Through this result, we can prove that our leaving protocol provides group forward secrecy.
- e) Group Backward Secrecy: Our joining protocol provides group backward secrecy when a user joins the group; namely, the  $U_{n+1}$  cannot compute the preceding group key. In our protocol, all the  $k_i$ 's changes for each session, so  $U_{n+1}$  cannot extract these values using the previous transcript. A joining member must compute  $k_i$  again with gathered information to compute the previous group key, but it is impossible to extract  $k_i$  from  $k'_i = H_2(g(k_i)r_ir_{i+1}P)$ . Hence, joining members cannot compute previous group keys, and our joining protocol provides group backward secrecy.
- f) Perfect Forward Secrecy: In our protocol, the computation of  $k_i$  needs public/private

Protocol	An onymity	Unlink	KS	FS	BS	PFS	EA
[CHL04]	X	X	0	О	О	0	Δ
[KKHY04]	X	х	х	0	0	х	Δ
[ZSM06]-2	X	X	0	0	0	X	Δ
[CHL08]	X	X	0	0	0	0	0
[YWJ08]	X	X	0	0	0	0	0
[WRLP08]	О	О	0	х	X	0	Δ
[PAK09]	X	х	0	О	0	X	0
Ours	О	О	0	0	0	0	0

Table 6.1: Security Requirements

key pair and  $r_i r_{i+1} P$ . Although the adversary reveals the private key  $S_i$ , he cannot compute  $k_i$  because computing  $r_i r_{i+1} P$  given  $\langle P, r_i P, r_{i+1} P \rangle$  is hard problem under the ECDH assumption. In means that our protocol provides perfect forward secrecy that revealing long-term keying material does not affect the secrecy of the established keys from previous sessions.

g) Entity Authentication: When the group members broadcast  $X_i$ 's in Wan et al.'s protocols, they verify that value with only the pseudonym  $Nym_i$ . This verification causes user impersonation of the malicious participants who know the pseudonyms. If the group members generate ID-based signatures for  $X_i$  and the other members verify all the signatures, they can easily authenticate the other users. Therefore, our protocol can provide entity authentication with the verification of the ID-based signatures that we recommended in Section 4.2. (In this case, the security by entity authentication depends on the security of the ID-based signature.)

In Section 2.1, several security requirements for GKA are defined. As previously explained, the protocol security can be defined with the definition of adversaries, passive or active adversaries, who want to interrupt or break the protocols. Table 6.1 shows that whether the GKA protocols reviewed in previous Sections and our protocol satisfy the requirements or not. "o" means the protocol satisfies the requirement, "x" means the protocol does not satisfies it, and " $\triangle$ " means the protocol tried to provide, but is incomplete. For example, if the protocol has  $\triangle$  in Entity Authentication than it provides the authentication but suffers from attack. We use the following notations:

Anonymity: Anonymity
Unlink: Unlinkability
KS: Key Secrecy
FS: Forward Secrecy

BS: Backward Secrecy

PFS: Perfect Forward Secrecy EA: Entity Authentication

In the Table 6.1, all the previous ID-based GKA protocols, which are reviewed in Chapter 3, do not provide anonymity and unlinkability. [WRLP08] protocols satisfy that requirements, but it suffers from impersonation attack, and does not provide forward and backward secrecy. In our protocols, impersonation attack is impossible because ID-based signature is used, and new/previous group members cannot extract group key for other sessions; i.e., all security requirements for GKA are satisfied. Therefore, security is enhanced in our proposed protocols.

#### 6.2 Performance



Table 6.2 shows the computational overhead of our protocols and other previous ID-based GKA protocols in joining/leaving operation. We use the following notations for comparison:

n: Number of group participants

ID: Number of ID-based encryption using  $Q_i / S_i$ Sig: Number of ID-based signature using  $Q_i / S_i$ Sym: Number of Symmetric encryption using KP: Number of pairing computation for each user

M: Number of multiplication for each user

B: Number of broadcast for each user

U: Number of unicast for each user

The previous ID-based GKA protocols had to operate all GKA protocol execution for each joining and leaving of the group member because any joining/leaving operation did not considered in their protocols. In [CHL08] and [YWJ08], which satisfy all security re-

Table 6.2: Computational overhead

	ID	Sig	Sym	E	P	M	В	U
[CHL04]	0	n	0	n(n-1)	4n	n(n+7)	2n	0
[KKHY04]	0	n	0	0	n(4n - 3)	n(n+4)	n	0
[ZSM06]-2	0	n	0	0	2(n - 1)	$n^2 + 5n - 2$	n	0
[CHL08]	0	2n	0	n(n-1)	6n	n(n + 10)	2n	0
[YWJ08]	0	2n	0	0	n(n+5)	2n(n+3)	3n	0
[PAK09]	0	n	0	0	3n	7n-1	n	0
Join								
[WRLP08]	3	3	1	0	4	4	1	6
Ours	1	n+2	1	0	4	2n+3	n+1	3
Leave								
[WRLP08]	0	2	2	0	2	4	0	4
Ours	0	n	1	0	2	2(n+1)	n+1	2

quirements except anonymity and unlinkability, many multiplication and pairing computations are required. Our protocols only require linear time of multiplication, and constant time of pairing computation. It means that our joining and leaving protocols enhance the performance compared with the previous protocols.

Tables 6.3 and 6.4 show the comparison of Wan et al.'s protocols [11] and our protocols for each participant in the group. Although all users should compute their  $k_i$  for each session in our joining/leaving protocols, the computation of new  $k_i$  requires only 2 scalar multiplications, 1 division, and 1 broadcasting, which is much smaller than the computation of [WRLP08-GKA] protocol. Moreover, in [WRLP08-Join] protocol,  $U_1$  should compute 4 encryptions for generating new session group key, but only 2 encryptions are required in our joining protocol. Therefore, our joining/leaving protocols does not increase much computational overhead from [WRLP08] protocols.

Table 6.3: Computational overhead in joining

Table 0.0. Compatitional overhead in Johning										
		ID	Sig	Sym	P	M	B	U		
	$U_1$	3	3	1	1	1	1	3		
WRLP08	$U_n$	0	0	0	1	1	0	1		
	$U_{n+1}$	0	0	0	2	2	0	2		
	$U_1$	1	2	1	1	2	2	1		
Ours	$U_n$	0	1	0	1	2	1	0		
	$U_{n+1}$	0	1	0	2	2	0	2		
	$U_i (i \neq 1, n, n+1)$	0	1	0	0	2	1	0		



Table 6.4: Computational overhead in leaving

	able 6.4. Compat	ID	Sig	Sym	P	M	В	U
WRLP08	$U_1$	0	2	2	0	0	0	2
	$U_{l\pm 1}$	0	0	0	1	2	0	2
	$U_1$	0	1	1	0	2	2	0
Ours	$U_{l\pm 1}$	0	1	0	1	3	1	1
	$U_i (i \neq 1, l \pm 1)$	0	1	0	0	2	1	0

## 7. Conclusion

In this paper, we found security weaknesses in Wan et al.'s ID-based GKA protocol and joining/leaving protocols: the GKA protocol suffers from insider colluding attack, and joining/leaving protocols cannot guarantee group backward/forward secrecy. We recommended using the ID-based signature to prevent the impersonation attack on the GKA protocol, and proposed our joining/leaving protocols. In our protocols, all the group members have to recompute individual secret,  $k_i$ , for each session to generate a new session group key, so joining or leaving members cannot obtain the previous or later session group key using the given individual secrets. In other words, our protocols can provide group forward/backward secrecy. Additionally, our joining/leaving protocols can operate efficiently compared with the [WRLP08] and other previous ID-based GKA protocols. With the our proposed joining/leaving protocols and the GKA protocol containing ID-based signature, the security can be enhanced while comparable efficiency is maintained.



# 요약문

#### 익명성을 제공하는 신원 기반 그룹 키 합의 프로토콜에 대한 연구

최근 인터넷 회의 또는 채팅 시스템에서는 안전하고 신뢰성 있는 통신을 위한 그룹 키 합의 (GKA) 프로토콜이 중요시 되고 있다. 그룹의 구성원들은 GKA 프로토콜을 이용 하여 하나의 비밀 키를 공유하고, 이 키를 이용하여 상호간에 전송되는 메시지를 암호화 또는 복호화 한다. 기존의 GKA 프로토콜들은 공개 키 암호 알고리즘을 기반으로 하여 그룹 비밀 키를 생성했는데, 이 경우 사용자의 공개 키를 생성, 관리, 인증, 삭제하는 등 별도의 관리가 필요했다. 그리하여 최근에는 그룹 구성원의 ID를 공개키로 사용하는 ID 기반 GKA 프로토콜 (ID-based GKA)에 대한 연구가 지속적으로 진행되고 있다. 하지만 ID 기반 GKA프로토콜에서는 외부 공격자가 어떤 특정 그룹에 속해있는 사용자의 ID를 쉽게 알아낼 수 있어 그룹 구성원의 익명성을 보장해주지 못한다는 단점이 있다. 2008년 Wan et al.은 이러한 단점을 보완하여 그룹 구성원의 익명성을 보장할 수 있는 ID기반 GKA 프로토콜과 동적 환경에서 사용자가 가입 또는 탈퇴하는 경우의 효율적인 프로토 콜을 제안하였다. 본 학위논문에서는 Wan et al.의 GKA 프로토콜이 공모된 사용자에 의 한 신원 위장 공격에 취약하다는 것과, 가입/탈퇴 프로토콜이 전방향 및 역방향 안전성을 만족시키지 못한다는 것을 증명하고, 이러한 취약점을 보완한 새로운 가입/탈퇴 프로토 콜을 제안하고자 한다. 제안된 프로토콜에서는 모든 그룹 구성원이 간단한 연산을 통해 새로운 개인 비밀 정보를 생성하고 이를 이용하여 동적 그룹에서의 새 그룹 키를 생성하 기 때문에, 가입 또는 탈퇴 구성원이 자신이 속해 있는 세션 이외 다른 세션의 그룹 키를 계산할 수 없다. 또한 신원 기반 서명을 메시지에 추가하여 공모에 의한 위장 공격이 불 가능하도록 설계되었다. 그러므로 제안된 프로토콜은 전방향 및 역방향 안전성을 만족시 키면서 공모된 사용자의 위장 공격 또한 막을 수 있다. 성능 면에서도 본 논문의 프로토 콜은 이전의 프로토콜들과 비교했을 때 효율성이 크게 떨어지지 않는다는 장점을 가지고 있다.

#### References

- A. Shamir, Identity-based Cryptosystems and Signature Schemes, Advances in Cryptology-Crypto 84, LNCS 196, pp.47-53, Springer-Verlag, 1984.
- [2] D. Boneh and M. Franklin, *Identity-based encryption from the Weil pairing*, Proc. of Crypto'01, LNCS 2139, pp.213-229, Springer-Verlag, 2001.
- [3] F. Zhang and X. Chen, Attack on Two ID-based Authenticated Group Key Agreement Schemes, Cryptology ePrint Archive: Report 2003/259.
- [4] K. Choi, J. Hwang and D. Lee, Efficient ID-based Group Key Agreement with Bilinear Maps, PKC'04, LNCS 2947, pp.130-144, Springer-Verlag, 2004.
- [5] J. Cheon, and Y. Kim, H. Yoon, A New ID-based Signature with Batch Verification, Cryptology ePrint Archive, Report 2004/131.
- [6] J. S. Kim, H. C. Kim, K. J. Ha and K. Y. Yoo, One Round Identity-Based Authenticated Conference Agreement Protocol, ECUMN 2004, LNCS 3262, pp. 407-416, Springer-Verlag, 2004.
- [7] M. Manulis, Survey on Security Requirements and Models for Group Key Exchange, Technical Report 2006/02, Horst-Gortz Institute, November 2006.
- [8] L. Zhou, W. Susilo and Y. Mu, Efficient ID-based Authenticated Group Key Agreement from Bilinear Pairings, Mobile Ad-hoc and Sensor Networks -MSN 2006, LNCS 4325, pp. 521-532, Springer-Verlag, 2006.
- [9] K. Shim, Further Analysis of ID-Based Authenticated Group Key Agreement Protocol from Bilinear Maps, IEICE Trans. Fundamentals, vol.E90-A, no.1, pp.231-233, 2007.
- [10] K. Choi, J. Hwang and D. Lee, ID-Based Authenticated Group Key Agreement Secure against Insider Attacks, IEICE Trans. Fundamentals, vol.E91-A, no.7, pp.1828-1830, 2008.
- [11] Z. Wan, K. Ren, W. Lou and B. Preneel, Anonymous ID-based Group Key Agreement for Wireless Networks, Wireless Communications and Networking Conference-2008 (WCNC 2008), IEEE, pp.2615-2620, 2008.

- [12] G. Yao, H. Wang and Q. Jiang, An Authenticated 3-Round Identity-Based Group Key Agreement Protocol, In proc. of the third International Conference on Availability, Reliability, and Security -ARES'08, pp. 538-543, ACM, 2008.
- [13] H. Park, T. Asano and K. Kim, Improved ID-based Authenticated Group Key Agreement Secure Against Impersonation Attack by Insider, 2009 Symposium on Cryptography and Information Security (SCIS 2009), Jan. 20-23, 2009.

